

$$\begin{cases} 2^x \cdot 3^y = 72 \\ 2^y \cdot 3^x = 108 \end{cases}$$

$$x = ?$$

$$y = ?$$

----- Q U E S T I O N -----

$$\begin{array}{|l} 2^x \cdot 3^y = 72 \\ 2^y \cdot 3^x = 108 \end{array}$$

$$x = ?$$

$$y = ?$$

----- R É P O N S E (proposée par GF) -----

Note: L1, L2, L3 ... = numéros des lignes dans un système d'équations.

$$\begin{array}{|l} \text{L1: } 2^x \cdot 3^y = 72 \\ \text{L2: } 2^y \cdot 3^x = 108 \end{array}$$

----- L1 -----

$$2^x \cdot 3^y = 72$$

$$\log[2](3) = 1,58496$$

$$\log[2](72) = 6,16992$$

$$2^x \cdot 2^{(1,58496y)} = 2^{6,16992}$$

$$2^{(x + 1,58496y)} = 2^{6,16992}$$

même base (= 2), donc:

$$x + 1,58496y = 6,16992 \quad \text{---> L3}$$

----- L2 -----

$$2^y \cdot 3^x = 108$$

$$3^x \cdot 2^y = 108$$

$$\log[3](2) = 0,63092$$

$$\log[3](108) = 4,26185$$

$$3^x \cdot 3^{(0,63092y)} = 3^{4,26185}$$

$$3^{(x + 0,63092y)} = 3^{4,26185}$$

même base (= 3), donc:

$$x + 0,63092y = 4,26185 \quad \text{---> L4}$$

----- L3 et L4 -----

$$\left| \begin{array}{l} \text{L3: } x + 1,58496y = 6,16992 \\ \text{L4: } x + 0,63092y = 4,26185 \end{array} \right|$$

$$\text{L3} - \text{L4: } (x + 1,58496y) - (x + 0,63092y) = 6,16992 - 4,26185$$

$$x + 1,58496y - x - 0,63092y = 6,16992 - 4,26185$$

$$x - x + 1,58496y - 0,63092y = 6,16992 - 4,26185$$

$$0,95404y = 1,90807$$

$$y = 1,90807/0,95404$$

$$\left| \begin{array}{l} \dots\dots\dots \\ y = 1,99999 = 2 \\ \dots\dots\dots \end{array} \right|$$

$$x + 1,58496y = 6,16992$$

$$x + 1,58496 \cdot 2 = 6,16992$$

$$x + 3,16992 = 6,16992$$

$$x = 6,16992 - 3,16992$$

$$\left| \begin{array}{l} \dots\dots\dots \\ x = 3 \\ \dots\dots\dots \end{array} \right|$$

----- R É P O N S E (vue sur YouTube) -----

Note: L1, L2, L3 ... = numéros des lignes dans un système d'équations.

----- L1·L2 -----

$$\begin{array}{|l} \text{L1: } 2^x \cdot 3^y = 72 \\ \text{L2: } 2^y \cdot 3^x = 108 \end{array}$$

$$\text{L1} \cdot \text{L2: } 2^x \cdot 3^y \cdot 2^y \cdot 3^x = 72 \cdot 108$$

$$2^x \cdot 2^y \cdot 3^y \cdot 3^x = 72 \cdot 108$$

$$2^{(x+y)} \cdot 3^{(x+y)} = 72 \cdot 108$$

$$(2 \cdot 3)^{(x+y)} = 72 \cdot 108$$

$$6^{(x+y)} = 72 \cdot 108$$

$$72 \cdot 108 = 2 \cdot 36 \cdot 3 \cdot 36$$

$$72 \cdot 108 = 2 \cdot 6^2 \cdot 3 \cdot 6^2$$

$$72 \cdot 108 = 6 \cdot 6^2 \cdot 6^2$$

$$72 \cdot 108 = 6^1 \cdot 6^2 \cdot 6^2$$

$$72 \cdot 108 = 6^{(1+2+2)}$$

$$72 \cdot 108 = 6^5$$

si $72 \cdot 108 = 6^5$ alors $6^{(x+y)} = 72 \cdot 108$ devient:

$$6^{(x+y)} = 6^5$$

même base (= 6), donc:

$$x + y = 5 \quad \text{---> L3}$$

----- L1/L2 -----

$$\begin{array}{|l} \text{L1: } 2^x \cdot 3^y = 72 \\ \text{L2: } 2^y \cdot 3^x = 108 \end{array}$$

$$\text{L1/L2: } (2^x \cdot 3^y) / (2^y \cdot 3^x) = 72/108$$

