

$$6^x + 9^x = 2^{(2x + 1)}$$

$x = ?$ (raisonnement)





QUESTION

$$6^x + 9^x = 2^{(2x + 1)}$$

$$x = ?$$

----- R É P O N S E -----

$$6^x + 9^x = 2^{(2x + 1)}$$

$$6^x + 9^x = 2^{(2x)} \cdot 2^1$$

$$6^x + 9^x = 2 \cdot 4^x$$

$$(6^x + 9^x)/4^x = 2$$

$$(6/4)^x + (9/4)^x = 2$$

$$(3/2)^x + (3/2)^{(2x)} = 2$$

$$(3/2)^x + ((3/2)^x)^2 = 2$$

$$\text{let } k = (3/2)^x$$

$$k + k^2 = 2$$

$$k^2 + k - 2 = 0$$

$$\Delta = 1^2 - 4 \cdot 1 \cdot (-2) = 1 + 8 = 9$$

$$\sqrt{\Delta} = \sqrt{9} = +3 \text{ et } \sqrt{9} = -3$$

- cas $\sqrt{\Delta} = +3$: $k = (-1 + 3)/2 \cdot 1 = 2/2 = 1$

- cas $\sqrt{\Delta} = -3$: $k = (-1 - 3)/2 \cdot 1 = -4/2 = -2$

----- $k = 1$ -----

$$k = (3/2)^x$$

$$1 = (3/2)^x$$

$$x = 0$$

----- $k = -2$ -----

$$k = (3/2)^x$$

$$-2 = (3/2)^x$$

pas de solution

----- résultat final -----

$$\begin{array}{c} \text{-----} \\ | \quad x = 0 \quad | \\ \text{-----} \end{array}$$