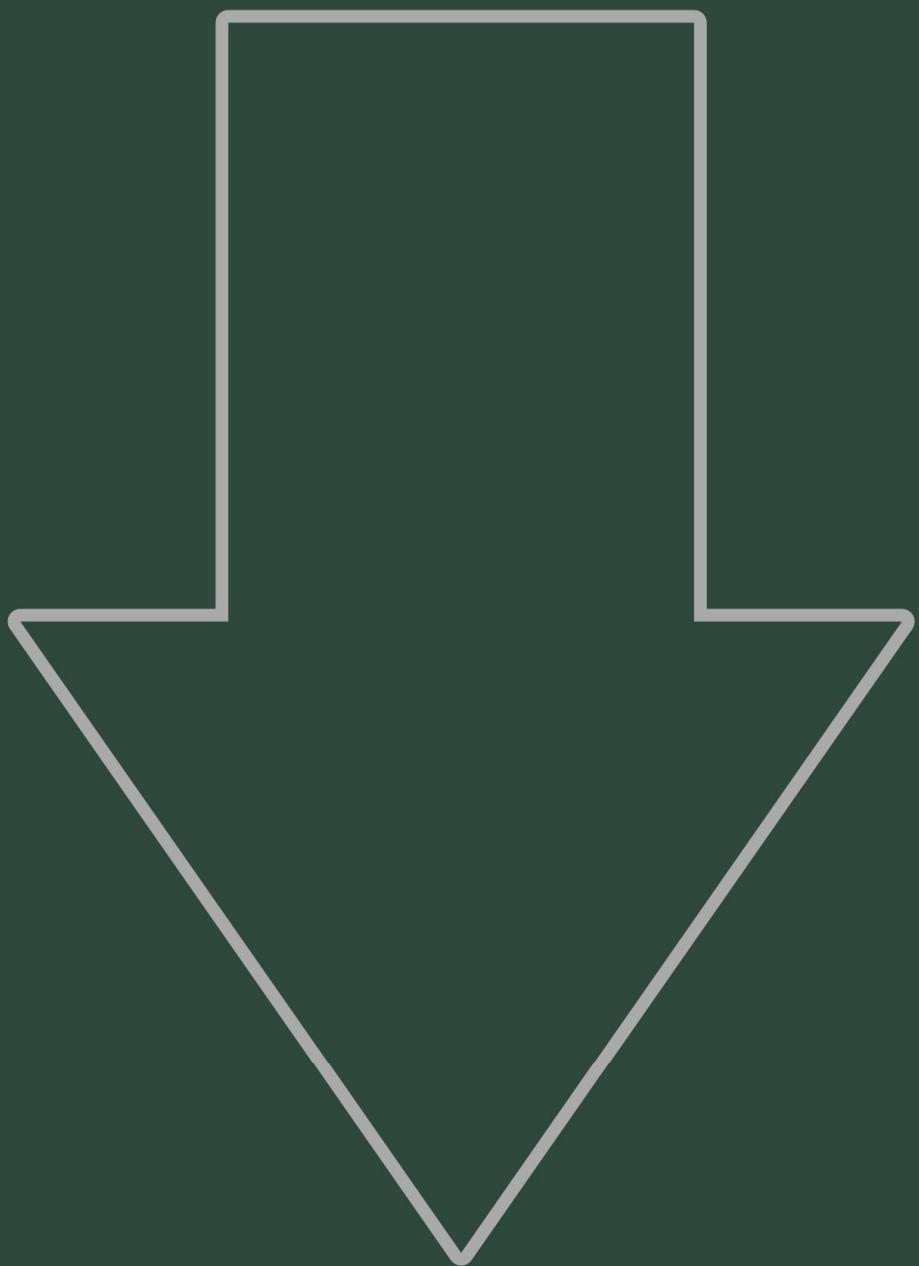




$$\begin{cases} 3^x - 3^y = 3 \\ 3^{x+y} = 3 \end{cases}$$

$x = ?$ et $y = ?$



----- Q U E S T I O N -----

| $3^x - 3^y = 3$

| $3^{(x+y)} = 3$

$x = ?$ et $y = ?$

----- R É P O N S E -----

| $3^x - 3^y = 3$

| $3^{(x+y)} = 3$

| $3^x - 3^y = 3$

| $3^x \cdot 3^y = 3$

soit:

• $3^x = a$

• $-(3^y) = b$

| $a + b = 3$

| $ab = -3$

rappel (système "somme et produit"):

• si S est la somme de a avec b

• si P est le produit de a avec b

• alors les racines de $z^2 - Sz + P = 0$ sont a et b

| $a + b = 3 = S$

| $ab = -3 = P$

$z^2 - 3z - 3 = 0$

$\Delta = (-3)^2 - 4 \cdot 1 \cdot (-3) = 9 + 12 = 21$

$\sqrt{\Delta} = +/- \sqrt{21}$

• cas $\sqrt{\Delta} = +\sqrt{21}$: $a = (-(-3) + \sqrt{21})/2 \cdot 1 = 3/2 + \sqrt{21}/2$

• cas $\sqrt{\Delta} = -\sqrt{21}$: $b = (-(-3) - \sqrt{21})/2 \cdot 1 = 3/2 - \sqrt{21}/2$

(voir page suivante)

----- 3^x = a -----

$$3^x = a = 3/2 + \sqrt{21}/2$$

$$3^x = 3/2 + \sqrt{21}/2$$

$$x = \log(3/2 + \sqrt{21}/2)/\log(3)$$

$$\begin{array}{|c|} \hline | & x \approx 1,213081 & | \\ \hline \end{array}$$

----- -3^y = b -----

$$-3^y = b = 3/2 - \sqrt{21}/2$$

$$-3^y = 3/2 - \sqrt{21}/2$$

$$3^y = \sqrt{21}/2 - 3/2$$

$$y = \log(\sqrt{21}/2 - 3/2)/\log(3)$$

$$\begin{array}{|c|} \hline | & y \approx -0,213081 & | \\ \hline \end{array}$$

----- Vérification -----

$$3^x - 3^y = 3$$

$$3^{1,213081} - 3^{-0,213081} = 2,999999 <---- \text{ok}$$

$$3^{(x + y)} = 3$$

$$3^{(1,213081 + -0,213081)} = 3^1$$

$$3^1 = 3 <---- \text{ok}$$

(fin)